

VERSION 6.0

**IMSL**<sup>™</sup>  
C Numerical Library

Function Catalog

## IMSL C Numerical Library

## Version 6.0

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# IMSL™ C NUMERICAL LIBRARY VERSION 6.0

For C and C++ programmers, providing the broadest coverage available of numerical subroutines written in native C.

At the heart of the IMSL C Numerical Library is a comprehensive set of pre-built mathematical and statistical analysis functions that programmers can embed directly into their numerical analysis applications. The IMSL C Numerical Library provides building blocks that eliminate the need to write code from scratch. These prepackaged functions allow developers to apply industry-specific expertise and reduce development time.

## COST-EFFECTIVENESS AND VALUE

The IMSL C Numerical Library significantly shortens program development time and promotes standardization. Variable argument lists have been implemented to simplify calling sequences. The IMSL C Library saves time in source code development and saves thousands of dollars in the design, development, documentation, testing and maintenance of applications.

## USER-FRIENDLY NOMENCLATURE

The IMSL C Library uses descriptive, explanatory function names for intuitive programming. Reserved function names begin with prefixes unique to each product.

Where appropriate, consistent variable names are used to:

- Make function names easy to identify, use, and prevent conflicts with other software
- Provide a common root name for numerical functions that offer the choice of multiple precisions

## ERROR HANDLING

Diagnostic error messages are clear and informative – designed not only to convey the error condition but also to suggest corrective action if appropriate.

These error-handling features:

- Make it faster and easier to debug programs
- Provide for more productive programming and confidence that the algorithms are functioning properly in an application

## PROGRAMMING INTERFACE FLEXIBILITY

The IMSL C Library takes full advantage of the intrinsic characteristics and desirable features of the C language. The functions support variable-length argument lists. The concise set of required arguments contains only information necessary for usage. Optional arguments provide added functionality and power to each function.

This flexibility:

- Reduces unnecessary code
- Enables the user to tailor each function call to specific program requirements.

## WIDE COMPATIBILITY AND UNIFORM OPERATION

With the IMSL Library, it is easy to build applications that are portable across multiple platforms. The IMSL C Library is available for a wide selection of UNIX/Linux and Windows computing environments.

Visual Numerics' commitment to regular feature and enhancement updates:

- Ensures that software will perform to the highest standards
- Provides for portable applications
- Assures that Visual Numerics will keep pace with the latest hardware and software innovations

## SHARED LIBRARY TECHNOLOGY

The IMSL C Library is designed to take advantage of shared libraries technology.

This technology:

- Allows more than one user to share code in the library thus minimizing disk space usage
- Provides shorter link time
- Minimizes the size of executable object modules

## THREAD SAFETY

The IMSL C Library is thread safe. Thread safety allows it to be used in multithreaded applications ranging from web-based applications to performing advanced data analysis in real time. This provides increased throughput, better response time, conservation of system resources and a natural programming structure. Performance benefits can be realized through concurrent and/or parallel execution.

## SMP ENABLED

The IMSL C Library has also been designed to take advantage of symmetric multiprocessor (SMP) systems. Computationally intensive algorithms in areas such as linear algebra and fast Fourier transforms will leverage SMP capabilities on a variety of systems.

## COMPREHENSIVE DOCUMENTATION

Documentation for the IMSL C Library is comprehensive, clearly written and standardized:

- Provides organized, easy-to-find information
- Documents, explains, and provides references for algorithms
- Gives at least one example of function usage, with sample input and results

## UNMATCHED PRODUCT SUPPORT

Behind every Visual Numerics' license is a team of professionals ready to provide expert answers to questions about the IMSL family of products. Product support options include product maintenance, ensuring the value and performance of IMSL software.

Product support:

- Gives users direct access to Visual Numerics' resident staff of expert product support specialists
- Provides prompt, two-way communication with solutions to a user's programming needs
- Includes product maintenance updates

## PROFESSIONAL SERVICES

Visual Numerics offers expert professional services for algorithm as well as complete application development. Please contact Visual Numerics to learn more about its extensive experience in developing custom algorithms, building algorithms in scalable platforms, and full applications development.

## Mathematical Functionality

The IMSL C Numerical Library is a collection of the most commonly required numerical functions, tailored for a C programmer's needs. The mathematical functionality is organized into 10 sections. These capabilities range from solving systems of linear equations to optimization.

**Linear Systems**, including real and complex full and sparse matrices, linear least squares, matrix decompositions, generalized inverses and vector-matrix operations.

**Eigensystem Analysis**, including eigenvalues and eigenvectors of complex, real symmetric and complex Hermitian matrices.

**Interpolation and Approximation**, including constrained curve-fitting splines, cubic splines, least squares approximation and smoothing, and scattered data interpolation.

**Integration and Differentiation**, including univariate, multivariate and Gauss quadrature.

**Differential Equations**, using Adams-Gear and Runge-Kutta methods for stiff and nonstiff ordinary differential equations and support for partial differential equations.

**Transforms**, including real and complex one- and two-dimensional fast Fourier transforms, as well as convolutions and correlations and Laplace transforms.

**Nonlinear Equations**, including zeros and root finding of polynomials, zeros of a function and root of a system of equations.

**Optimization**, including unconstrained, and linearly and nonlinearly constrained minimizations.

**Special Functions**, including error and gamma functions, real order complex valued Bessel functions, statistical functions.

- *Financial Functions*, including functions for Bond and cash-flow analysis.

**Utilities**, including CPU time used, error handling and machine, mathematical, physical constants, retrieval of machine constants, changing error handling defaults, and performing matrix-matrix multiplication.

## Statistical Functionality

The statistical functionality is organized into 13 sections. These capabilities range from analysis of variance to random number generation.

**Basic Statistics**, including univariate summary statistics, nonparametric tests, such as sign and Wilcoxon rank sum, and goodness-of-fit tests, such as chi-squared and Shapiro-Wilks' tests.

**Regression**, including stepwise regression, all best regression, multiple linear regression models, polynomial models and nonlinear models.

**Correlation and Covariance**, including sample variance-covariance, partial correlation and covariances, pooled variance-covariance and robust estimates of a covariance matrix and mean factor.

**Analysis of Variance and Designed Experiments**, including Yates' method for estimating missing observations in designed experiments, analysis of hierarchical data, analysis of standard factorial experiments, randomized completed block designs, latin-square, lattice, split-plot, strip-plot, split-split plot and strip-split plot experiments, and standard tests for multiple comparisons of treatment means and homogeneity of variance.

**Categorical and Discrete Data Analysis**, including chi-squared analysis of a two-way contingency table, exact probabilities in a two-way contingency table and analysis of categorical data using general linear models, including logistic regression.

**Nonparametric Statistics**, including sign tests, Wilcoxon rank sum tests and Cochran's Q test for related observations.

**Tests of Goodness-of-Fit**, including chi-squared goodness-of-fit tests, Kolmogorov/Smirnov tests and tests for normality.

**Time Series Analysis and Forecasting**, including analysis and forecasting of time series using a nonseasonal ARMA model, GARCH (Generalized Autoregressive Conditional Heteroskedasticity), Kalman filtering, portmanteau lack of fit test and difference of a seasonal or nonseasonal time series.

**Multivariate Analysis**, including principal component analysis, discriminant analysis, K-means and hierarchical cluster analysis and factor analysis. Methods of factor analysis include principal components, principal factor, image analysis, unweighted least squares, generalized least squares, maximum likelihood, and various factor rotations.

**Survival Analysis**, including analysis of data using the Cox linear survival model, Kaplan-Meier survival estimates, actuarial survival tables, and non-parametric survival estimates.

**Probability Distribution Functions and Inverses**, including binomial, hypergeometric, bivariate normal, gamma and many more.

**Random Number Generation**, including a generator for multivariate normal distributions and pseudorandom numbers from several distributions, including gamma, Poisson and beta. Also, support for low discrepancy series using a generalized Faure sequence.

**Data Mining**, including feed forward neural networks, plus neural network data pre- and post-processing algorithms, are particularly well suited to developing predictive models in noisy or challenging data situations.

## IMSL – Also Available for JAVA™, C# and Fortran

### JMSL™ NUMERICAL LIBRARY FOR JAVA PROGRAMMERS

The JMSL Numerical Library is a pure Java numerical library that operates in the Java J2SE or J2EE frameworks. The library extends core Java numerics and allows developers to seamlessly integrate advanced mathematical, statistical, financial, and charting functions into their Java applications. To build this library, Visual Numerics has taken individual algorithms and re-implemented them as object-oriented, Java classes. The JMSL Library is 100% pure Java and, like all Visual Numerics products, is fully tested and documented, with code examples included. The JMSL Library also adds financial functions and charting to the library, taking advantage of the collaboration and graphical benefits of Java. The JMSL Library is designed with extensibility in mind; new classes may be derived from existing ones to add functionality to satisfy particular requirements. The JMSL Library can provide advanced mathematics in client-side applets, server-side applications or even non-networked desktop applications. JMSL applets perform all processing on the Java client, whether it is a thin client, such as a network computer, a PC or workstation equipped with a Java Virtual Machine. Client-side processing reduces the number of “round trips” to a networked server, which in turn minimizes network traffic and system latency.

### IMSL C# NUMERICAL LIBRARY

The IMSL C# Library is a 100% C# analytics library, providing broad coverage of advanced mathematics and statistics for the Microsoft® .NET Framework. The IMSL C# Library delivers a new level of embeddable and scalable analytics capability to Visual Studio™ users that was once only found in traditional high performance computing environments. This offers C# and Visual Basic.NET (VB.NET) developers seamless accessibility to advanced analytics capabilities in the most integrated language for the .NET environment with the highest degree of programming productivity and ease of use with Visual Studio. Visual Numerics has taken C# to a new level by extending the mathematical framework of the language, significantly increasing the high performance analytics capabilities available for the .NET Framework. Classes such as a complex numbers class, a matrix class, as well as advanced random number generator classes provide a foundation from which advanced mathematics can be built.

### IMSL FORTRAN NUMERICAL LIBRARY AND IMSL THREAD SAFE FORTRAN NUMERICAL LIBRARY

The IMSL Fortran Library is used by technical professionals for high performance computing engineering, and education applications. The IMSL Fortran Library is a single package that incorporates all of the algorithms and features from the IMSL family of Fortran libraries. The IMSL Fortran Library allows users to utilize the fast, convenient optional arguments of the modern Fortran syntax throughout the library, in all areas where optional arguments can apply, while maintaining full backward compatibility. The IMSL Thread Safe Fortran Library is a 100% thread safe edition of the entire IMSL Fortran Library allowing the convenience and performance of multi-threading on selected environments. The IMSL Fortran Library and the IMSL Thread Safe Fortran Library include all of the algorithms from the IMSL family of Fortran libraries including the former IMSL F90 Library, the IMSL Fortran 77 Library, and the IMSL parallel processing features.

## CHAPTER 1: LINEAR SYSTEMS

### LINEAR EQUATIONS WITH FULL MATRICES:

<code>lin_sol_gen</code>	Solves a real general system of linear equations $Ax = b$ .
<code>lin_sol_gen (complex)</code>	Solves a complex general system of linear equations $Ax = b$ .
<code>lin_sol_posdef</code>	Solves a real symmetric positive definite system of linear equations $Ax = b$ .
<code>lin_sol_posdef (complex)</code>	Solves a complex Hermitian positive definite system of linear equations $Ax = b$ .

### LINEAR EQUATIONS WITH BAND MATRICES:

<code>lin_sol_gen_band</code>	Solves a real general band system of linear equations $Ax = b$ .
<code>lin_sol_gen_band (complex)</code>	Solves a complex general band system of linear equations $Ax = b$ .
<code>lin_sol_posdef_band</code>	Solves a real symmetric positive definite system of linear equations $Ax = b$ in band symmetric storage mode.
<code>lin_sol_posdef_band (complex)</code>	Solves a complex Hermitian positive definite system of linear equations $Ax = b$ in band symmetric storage mode.

### LINEAR EQUATIONS WITH GENERAL SPARSE MATRICES:

<code>lin_sol_gen_coordinate</code>	Solves a sparse system of linear equations $Ax = b$ .
<code>lin_sol_gen_coordinate (complex)</code>	Solves a sparse system of linear equations $Ax = b$ , with sparse complex coefficient matrix $A$ .
<code>lin_sol_posdef_coordinate</code>	Solves a sparse real symmetric positive definite system of linear equations $Ax = b$ .
<code>lin_sol_posdef_coordinate (complex)</code>	Solves a sparse Hermitian positive definite system of linear equations $Ax = b$ .

### ITERATIVE METHODS:

<code>lin_sol_gen_min_residual</code>	Solves a linear system $Ax = b$ using the restarted generalized minimum residual (GMRES) method.
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ITERATIVE METHODS: (con't)

`lin_sol_def_cg` Solves a real symmetric definite linear system using a conjugate gradient method.

**LINEAR LEAST-SQUARES WITH FULL MATRICES:**

`lin_least_squares_gen` Solves a linear least-squares problem  $Ax = b$ .

`lin_lsq_lin_constraints` Solves a linear least squares problem with linear constraints.

`lin_svd_gen` Computes the SVD,  $A = USV^T$ , of a real rectangular matrix  $A$ .

`lin_svd_gen (complex)` Computes the SVD,  $A = USV^H$ , of a complex rectangular matrix  $A$ .

`lin_sol_nonnegdef` Solves a real symmetric nonnegative definite system of linear equations  $Ax = b$ .

**CHAPTER 2: EIGENSYSTEM ANALYSIS****LINEAR EIGENSYSTEM PROBLEMS:**

`eig_gen` Computes the eigenexpansion of a real matrix  $A$ .

`eig_gen (complex)` Computes the eigenexpansion of a complex matrix  $A$ .

`eig_sym` Computes the eigenexpansion of a real symmetric matrix  $A$ .

`eig_herm (complex)` Computes the eigenexpansion of a complex Hermitian matrix  $A$ .

**GENERALIZED EIGENSYSTEM PROBLEMS:**

`eig_symgen` Computes the generalized eigenexpansion of a system  $Ax = \lambda Bx$ .  $A$  and  $B$  are real and symmetric.  $B$  is positive definite.

`geneig` Computes the generalized eigenexpansion of a system  $Ax = \lambda Bx$ , with  $A$  and  $B$  real.

`geneig (complex)` Computes the generalized eigenexpansion of a system  $Ax = \lambda Bx$ , with  $A$  and  $B$  complex.

**CHAPTER 3: INTERPOLATION AND APPROXIMATION****CUBIC SPLINE INTERPOLATION:**

`cub_spline_interp_e_cnd` Computes a cubic spline interpolant, specifying various endpoint conditions.

`cub_spline_interp_shape` Computes a shape-preserving cubic spline.

**CUBIC SPLINE EVALUATION AND INTEGRATION:**

<code>cub_spline_value</code>	Computes the value of a cubic spline or the value of one of its derivatives.
<code>cub_spline_integral</code>	Computes the integral of a cubic spline.

**SPLINE INTERPOLATION:**

<code>spline_interp</code>	Computes a spline interpolant.
<code>spline_knots</code>	Computes the knots for a spline interpolant.
<code>spline_2d_interp</code>	Computes a two-dimensional, tensor-product spline interpolant from two-dimensional, tensor-product data.

**SPLINE EVALUATION AND INTEGRATION:**

<code>spline_value</code>	Computes the value of a spline or the value of one of its derivatives.
<code>spline_integral</code>	Computes the integral of a spline.
<code>spline_2d_value</code>	Computes the value of a tensor-product spline or the value of one of its partial derivatives.
<code>spline_2d_integral</code>	Evaluates the integral of a tensor-product spline on a rectangular domain.

**LEAST-SQUARES APPROXIMATION AND SMOOTHING:**

<code>user_fcn_least_squares</code>	Computes a least-squares fit using user-supplied functions.
<code>spline_least_squares</code>	Computes a least-squares spline approximation.
<code>spline_2d_least_squares</code>	Computes a two-dimensional, tensor-product spline approximant using least squares.
<code>cub_spline_smooth</code>	Computes a smooth cubic spline approximation to noisy data by using cross-validation to estimate the smoothing parameter or by directly choosing the smoothing parameter.
<code>spline_lsq_constrained</code>	Computes a least-squares constrained spline approximation.
<code>smooth_1d_data</code>	Smooth one-dimensional data by error detection.

**SCATTERED DATA INTERPOLATION:**

<code>scattered_2d_interp</code>	Computes a smooth bivariate interpolant to scattered data that is locally a quintic polynomial in two variables.
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## SCATTERED DATA LEAST SQUARES:

radial\_scattered\_fit

Computes an approximation to scattered data in  $\mathbf{R}^n$  for  $n \leq 1$  using radial basis functions.

radial\_evaluate

Evaluates a radial basis fit.

## CHAPTER 4: QUADRATURE

## UNIVARIATE QUADRATURE:

int\_fcn\_sing

Integrates a function, which may have endpoint singularities, using a globally adaptive scheme based on Gauss-Kronrod rules.

int\_fcn

Integrates a function using a globally adaptive scheme based on Gauss-Kronrod rules.

int\_fcn\_sing\_pts

Integrates a function with singularity points given.

int\_fcn\_alg\_log

Integrates a function with algebraic-logarithmic singularities.

int\_fcn\_inf

Integrates a function over an infinite or semi-infinite interval.

int\_fcn\_trig

Integrates a function containing a sine or a cosine factor.

int\_fcn\_fourier

Computes a Fourier sine or cosine transform.

int\_fcn\_cauchy

Computes integrals of the form  $\int_a^b \frac{f(x)}{x-c} dx$  in the Cauchy principal value sense.

int\_fcn\_smooth

Integrates a smooth function using a nonadaptive rule.

## MULTIVARIATE QUADRATURE:

int\_fcn\_2d

Computes a two-dimensional iterated integral.

int\_fcn\_hyper\_rect

Integrates a function on a hyper-rectangle  $\int_{a_0}^{b_0} \dots \int_{a_{n-1}}^{b_{n-1}} f(x_0, \dots, x_{n-1}) dx_{n-1} \dots dx_0$ 

int\_fcn\_qmc

Integrates a function on a hyper-rectangle using a quasi-Monte Carlo method.

## GAUSS QUADRATURE:

gauss\_quad\_rule

Computes a Gauss, Gauss-Radau, or Gauss-Lobatto quadrature rule with various classical weight functions.

## DIFFERENTIATION:

fcn\_derivative

Computes the first, second or third derivative of a user-supplied function.

## CHAPTER 5: DIFFERENTIAL EQUATIONS

### RUNGE-KUTTA METHOD:

`ode_runge_kutta`

Solves an initial-value problem for ordinary differential equations using the Runge-Kutta-Verner fifth-order and sixth-order method.

### ADAM'S OR GEAR'S METHOD:

`ode_adams_gear`

Solves a stiff initial-value problem for ordinary differential equations using the Adams-Gear methods.

### PETZOLD-GEAR METHOD:

`dea_petzold_gear`

Solves a first order differential-algebraic system of equations,  $g(t, y, y^*) = 0$ , using the Petzold-Gear BDF method.

### PARTIAL DIFFERENTIAL EQUATIONS:

`pde_1d_mg`

Solves a system of one-dimensional time-dependent partial differential equations using a moving-grid interface.

### METHOD OF LINES:

`pde_method_of_lines`

Solves a system of partial differential equations of the form  $u_t = f(x, t, u, u_x, u_{xx})$  using the method of lines.

### BOUNDARY VALUE PROBLEM:

`bvp_finite_difference`

Solves a (parameterized) system of differential equations with boundary conditions at two points, using a variable order, variable step size, finite difference method with deferred corrections.

### FAST POISSON SOLVER:

`fast_poisson_2d`

Solves Poisson's or Helmholtz's equation on a two-dimensional rectangle using a fast Poisson solver based on the HODIE finite-difference scheme on a uniform mesh.

## CHAPTER 6: TRANSFORMS

### REAL TRIGONOMETRIC FFTS:

`fft_real`

Computes the real discrete Fourier transform of a real sequence.

`fft_real_init`

Computes the parameters for `imsl_f_fft_real`.

**COMPLEX EXPONENTIAL FFTS:**

`fft_complex` Computes the complex discrete Fourier transform of a complex sequence.

`fft_complex_init` Computes the parameters for `imsl_c_fft_complex`.

**REAL SINE AND COSINE FFTS:**

`fft_cosine` Computes the discrete Fourier cosine transformation of an even sequence.

`fft_cosine_init` Computes the parameters needed for `imsl_f_fft_cosine`.

`fft_sine` Computes the discrete Fourier sine transformation of an odd sequence.

`fft_sine_init` Computes the parameters needed for `imsl_f_fft_sine`.

**TWO-DIMENSIONAL FFTS:**

`fft_2d_complex` Computes the complex discrete two-dimensional Fourier transform of a complex two-dimensional array.

**CONVOLUTION AND CORRELATION:**

`convolution` Computes the convolution, and optionally, the correlation of two real vectors.

`convolution (complex)` Computes the convolution, and optionally, the correlation of two complex vectors.

**LAPLACE TRANSFORM:**

`inverse_laplace` Computes the inverse Laplace transform of a complex function.

**CHAPTER 7: NONLINEAR EQUATIONS****ZEROS OF A POLYNOMIAL:**

`zeros_poly` Finds the zeros of a polynomial with real coefficients using the Jenkins-Traub three-stage algorithm.

`zeros_poly (complex)` Finds the zeros of a polynomial with complex coefficients using the Jenkins-Traub three-stage algorithm.

**ZEROS OF A FUNCTION:**

`zeros_fcn` Finds the real zeros of a real function using Müller's method.

## ROOT OF A SYSTEM OF EQUATIONS:

`zeros_sys_eqn` Solves a system of  $n$  nonlinear equations  $f(x) = 0$  using a modified Powell hybrid algorithm.

## CHAPTER 8: OPTIMIZATION

## UNCONSTRAINED MINIMIZATION:

`min_uncon` Finds the minimum point of a smooth function  $f(x)$  of a single variable using only function evaluations.

`min_uncon_deriv` Finds the minimum point of a smooth function  $f(x)$  of a single variable using both function and first derivative evaluations.

`min_uncon_multivar` Minimizes a function  $f(x)$  of  $n$  variables using a quasi-Newton method.

`nonlin_least_squares` Solves a nonlinear least-squares problem using a modified Levenberg-Marquardt algorithm.

## LINEARLY CONSTRAINED MINIMIZATION:

`read_mps` Reads an MPS file containing a linear programming problem or a quadratic programming problem.

`linear_programming` Solves a linear programming problem.

`lin_prog` Solves a linear programming problem using the revised simplex algorithm.

`quadratic_prog` Solves a quadratic programming problem subject to linear equality or inequality constraints.

`min_con_gen_lin` Minimizes a general objective function subject to linear equality/inequality constraints.

`bounded_least_squares` Solves a nonlinear least-squares problem subject to bounds on the variables using a modified Levenberg-Marquardt algorithm.

## NONLINEARLY CONSTRAINED MINIMIZATION:

`constrained_nlp` Solves a general nonlinear programming problem using a sequential equality constrained quadratic programming method.

## CHAPTER 9: SPECIAL FUNCTIONS

## ERROR AND GAMMA FUNCTIONS:

`erf` Evaluates the real error function  $\text{erf}(x)$ .

`erfc` Evaluates the real complementary error function  $\text{erfc}(x)$ .

## ERROR AND GAMMA FUNCTIONS: (CONT)

<code>erf_inverse</code>	Evaluates the real inverse error function $\text{erf}^{-1}(x)$ .
<code>erfce</code>	Evaluates the exponentially scaled complementary error function.
<code>erfe</code>	Evaluates a scaled function related to $\text{erfc}(z)$ .
<code>erfc_inverse</code>	Evaluates the real inverse complementary error function $\text{erfc}^{-1}(x)$ .
<code>beta</code>	Evaluates the real beta function $\beta(x, y)$ .
<code>log_beta</code>	Evaluates the logarithm of the real beta function $\ln \beta(x, y)$ .
<code>beta_incomplete</code>	Evaluates the real incomplete beta function $I_x = \beta_x(a, b) / \beta(a, b)$ .
<code>gamma</code>	Evaluates the real gamma function $\Gamma(x)$ .
<code>log_gamma</code>	Evaluates the logarithm of the absolute value of the gamma function $\log  \Gamma(x) $ .
<code>gamma_incomplete</code>	Evaluates the incomplete gamma function $\gamma(a, x)$ .

**BESSEL FUNCTIONS:**

<code>bessel_J0</code>	Evaluates the real Bessel function of the first kind of order zero $J_0(x)$ .
<code>bessel_J1</code>	Evaluates the real Bessel function of the first kind of order one $J_1(x)$ .
<code>bessel_Jx</code>	Evaluates a sequence of Bessel functions of the first kind with real order and complex arguments.
<code>bessel_Y0</code>	Evaluates the real Bessel function of the second kind of order zero $Y_0(x)$ .
<code>bessel_Y1</code>	Evaluates the real Bessel function of the second kind of order one $Y_1(x)$ .
<code>bessel_Yx</code>	Evaluates a sequence of Bessel functions of the second kind with real order and complex arguments.
<code>bessel_I0</code>	Evaluates the real modified Bessel function of the first kind of order zero $I_0(x)$ .
<code>bessel_exp_I0</code>	Evaluates the exponentially scaled modified Bessel function of the first kind of order zero.
<code>bessel_I1</code>	Evaluates the real modified Bessel function of the first kind of order one $I_1(x)$ .
<code>bessel_exp_I1</code>	Evaluates the exponentially scaled modified Bessel function of the first kind of order one.
<code>bessel_Ix</code>	Evaluates a sequence of modified Bessel functions of the first kind with real order and complex arguments.
<code>bessel_K0</code>	Evaluates the real modified Bessel function of the second kind of order zero $K_0(x)$ .

BESSEL FUNCTIONS: (CONT)

bessel_exp_K0	Evaluates the exponentially scaled modified Bessel function of the second kind of order zero.
bessel_K1	Evaluates the real modified Bessel function of the second kind of order one $K_1(x)$ .
bessel_exp_K1	Evaluates the exponentially scaled modified Bessel function of the second kind of order one.
bessel_Kx	Evaluates a sequence of modified Bessel functions of the second kind with real order and complex arguments.

ELLIPTIC INTEGRALS:

elliptic_integral_K	Evaluates the complete elliptic integral of the kind $K(x)$ .
elliptic_integral_E	Evaluates the complete elliptic integral of the second kind $E(x)$ .
elliptic_integral_RF	Evaluates Carlson's elliptic integral of the first kind $R_F(x, y, z)$ .
elliptic_integral_RD	Evaluates Carlson's elliptic integral of the second kind $R_D(x, y, z)$ .
elliptic_integral_RJ	Evaluates Carlson's elliptic integral of the third kind $R_J(x, y, z, \rho)$ .
elliptic_integral_RC	Evaluates an elementary integral from which inverse circular functions, logarithms, and inverse hyperbolic functions can be computed.

FRESNEL INTEGRALS:

fresnel_integral_C	Evaluates the cosine Fresnel integral.
fresnel_integral_S	Evaluates the sine Fresnel integral.

AIRY FUNCTIONS:

airy_Ai	Evaluates the Airy function.
airy_Bi	Evaluates the Airy function of the second kind.
airy_Ai_derivative	Evaluates the derivative of the Airy function.
airy_Bi_derivative	Evaluates the derivative of the Airy function of the second kind.

KELVIN FUNCTIONS:

kelvin_ber0	Evaluates the Kelvin function of the first kind, ber, of order zero.
kelvin_bei0	Evaluates the Kelvin function of the first kind, bei, of order zero.
kelvin_ker0	Evaluates the Kelvin function of the second kind, ker, of order zero.

## KELVIN FUNCTIONS: (CONT)

kelvin_kei0	Evaluates the Kelvin function of the second kind, $kei$ , of order zero.
kelvin_ber0_derivative	Evaluates the derivative of the Kelvin function of the first kind, $ber$ , of order zero.
kelvin_bei0_derivative	Evaluates the derivative of the Kelvin function of the first kind, $bei$ , of order zero.
kelvin_ker0_derivative	Evaluates the derivative of the Kelvin function of the second kind, $ker$ , of order zero.
kelvin_kei0_derivative	Evaluates the derivative of the Kelvin function of the second kind, $kei$ , of order zero.

## STATISTICAL FUNCTIONS:

normal_cdf	Evaluates the standard normal (Gaussian) distribution function.
normal_inverse_cdf	Evaluates the inverse of the standard normal (Gaussian) distribution function.
chi_squared_cdf	Evaluates the chi-squared distribution function.
chi_squared_inverse_cdf	Evaluates the inverse of the chi-squared distribution function.
F_cdf	Evaluates the $F$ distribution function.
F_inverse_cdf	Evaluates the inverse of the $F$ distribution function.
t_cdf	Evaluates the Student's $t$ distribution function.
t_inverse_cdf	Evaluates the inverse of the Student's $t$ distribution function.
gamma_cdf	Evaluates the gamma distribution function.
binomial_cdf	Evaluates the binomial distribution function.
hypergeometric_cdf	Evaluates the hypergeometric distribution function.
poisson_cdf	Evaluates the Poisson distribution function.
beta_cdf	Evaluates the beta distribution function.
beta_inverse_cdf	Evaluates the inverse of the beta distribution function.
bivariate_normal_cdf	Evaluates the bivariate normal distribution function.

## FINANCIAL FUNCTIONS:

cumulative_interest	Evaluates the cumulative interest paid between two periods.
cumulative_principal	Evaluates the cumulative principal paid between two periods.

## FINANCIAL FUNCTIONS: (CONT)

<code>depreciation_db</code>	Evaluates the depreciation of an asset. (Fixed-declining balance method.)
<code>depreciation_ddb</code>	Evaluates the depreciation of an asset. (Double-declining balance method.)
<code>depreciation_sln</code>	Evaluates the depreciation of an asset. (Straight-line method.)
<code>depreciation_syd</code>	Evaluates the depreciation of an asset. (Sum-of-years digits method.)
<code>depreciation_vdb</code>	Evaluates the depreciation of an asset for any given period, including partial periods. (Variable-declining balance method.)
<code>dollar_decimal</code>	Converts a fractional price to a decimal price.
<code>dollar_fraction</code>	Converts a decimal price to a fractional price.
<code>effective_rate</code>	Evaluates the effective annual interest rate.
<code>future_value</code>	Evaluates an investment's future value.
<code>future_value_schedule</code>	Evaluates the future value of an initial principal taking into consideration a schedule of compound interest rates.
<code>interest_payment</code>	Evaluates the interest payment for an investment for a given period.
<code>interest_rate_annuity</code>	Evaluates an annuity's interest rate per period.
<code>internal_rate_of_return</code>	Evaluates the internal rate of return for a schedule of cash flows.
<code>internal_rate_schedule</code>	Evaluates the internal rate of return for a schedule of cash flows. It is not necessary that the cash flows be periodic.
<code>modified_internal_rate</code>	Evaluates the modified internal rate of return for a schedule of periodic cash flows.
<code>net_present_value</code>	Evaluates an investment's net present value. The calculation is based on a schedule of periodic cash flows and a discount rate.
<code>nominal_rate</code>	Evaluates the nominal annual interest rate.
<code>number_of_periods</code>	Evaluates the number of periods for an investment for which periodic and constant payments are made and the interest rate is constant.
<code>payment</code>	Evaluates the periodic payment for an investment.
<code>present_value</code>	Evaluates the net present value of a stream of equal periodic cash flows, which are subject to a given discount rate.
<code>present_value_schedule</code>	Evaluates the present value for a schedule of cash flows. It is not necessary that the cash flows be periodic.
<code>principal_payment</code>	Evaluates the payment on the principal for a specified period.

**BOND FUNCTIONS:**

<code>accr_interest_maturity</code>	Evaluates the interest that has accrued on a security, which pays interest at maturity.
<code>accr_interest_periodic</code>	Evaluates the interest that has accrued on a security, which pays interest periodically.
<code>bond_equivalent_yield</code>	Evaluates a Treasury bill's bond-equivalent yield.
<code>convexity</code>	Evaluates the convexity for a security.
<code>coupon_days</code>	Evaluates the number of days in the coupon period containing the settlement date.
<code>coupon_number</code>	Evaluates the number of coupons payable between the settlement date and the maturity date.
<code>days_before_settlement</code>	Evaluates the number of days starting with the beginning of the coupon period and ending with the settlement date.
<code>days_to_next_coupon</code>	Evaluates the number of days starting with the settlement date and ending with the next coupon date.
<code>depreciation_amordegrc</code>	Evaluates the depreciation for each accounting period. During the evaluation of the function a depreciation coefficient based on the asset life is applied.
<code>depreciation_amorlinc</code>	Evaluates the depreciation for each accounting period. This function is similar to <i>depreciation_amordegrc</i> , except that <i>depreciation_amordegrc</i> has a depreciation coefficient that is applied during the evaluation that is based on the asset life.
<code>discount_price</code>	Evaluates a discounted security's price per \$100 face value.
<code>discount_rate</code>	Evaluates a security's discount rate.
<code>discount_yield</code>	Evaluates a discounted security's annual yield.
<code>duration</code>	Evaluates a security's annual duration where the security has periodic interest payments.
<code>interest_rate_security</code>	Evaluates a fully invested security's interest rate.
<code>modified_duration</code>	Evaluates a security's modified Macauley duration assuming a par value of \$100.
<code>next_coupon_date</code>	Evaluates the first coupon date that follows the settlement date.
<code>previous_coupon_date</code>	Evaluates the coupon date that immediately precedes the settlement date.
<code>price</code>	Evaluates a security's price per \$100 face value. The security pays periodic interest.
<code>price_maturity</code>	Evaluates a security's price per \$100 face value. The security pays interest at maturity.
<code>received_maturity</code>	Evaluates the amount one receives when a fully invested security reaches the maturity date.
<code>treasury_bill_price</code>	Evaluates a Treasury bill's price per \$100 face value.

## BOND FUNCTIONS: (con't)

<code>treasury_bill_yield</code>	Evaluates a Treasury bill's yield.
<code>year_fraction</code>	Evaluates the fraction of a year represented by the number of whole days between two dates.
<code>yield_maturity</code>	Evaluates a security's annual yield. The security pays interest at maturity.
<code>yield_periodic</code>	Evaluates a security's yield. The security pays periodic interest.

## CHAPTER 10: STATISTICS AND RANDOM NUMBER GENERATION

## STATISTICS:

<code>simple_statistics</code>	Computes basic univariate statistics.
<code>table_oneway</code>	Tallies observations into a one-way frequency table.
<code>chi_squared_test</code>	Performs a chi-squared goodness-of-fit test.
<code>covariances</code>	Computes the sample variance-covariance or correlation matrix.
<code>regression</code>	Fits a multiple linear regression model using least squares.
<code>poly_regression</code>	Performs a polynomial least-squares regression.
<code>ranks</code>	Computes the ranks, normal scores, or exponential scores for a vector of observations.

## RANDOM NUMBERS:

<code>random_seed_get</code>	Retrieves the current value of the seed used in the IMSL random number generators.
<code>random_seed_set</code>	Initializes a random seed for use in the IMSL random number generators.
<code>random_option</code>	Selects the uniform (0, 1) multiplicative congruential pseudorandom number generator.
<code>random_uniform</code>	Generates pseudorandom numbers from a uniform (0, 1) distribution.
<code>random_normal</code>	Generates pseudorandom numbers from a standard normal distribution using an inverse CDF method.
<code>random_poisson</code>	Generates pseudorandom numbers from a Poisson distribution.
<code>random_gamma</code>	Generates pseudorandom numbers from a standard gamma distribution.
<code>random_beta</code>	Generates pseudorandom numbers from a beta distribution.
<code>random_exponential</code>	Generates pseudorandom numbers from a standard exponential distribution.

RANDOM NUMBERS: (con't)

`faure_next_point`

Computes a shuffled Faure sequence.

## CHAPTER 11: PRINTING FUNCTIONS

### PRINT:

`write_matrix`

Prints a rectangular matrix (or vector) stored in contiguous memory locations.

### SET:

`page`

Sets or retrieves the page width or length.

`write_options`

Sets or retrieves an option for printing a matrix.

## CHAPTER 12: UTILITIES

### SET OUTPUT FILES:

`output_file`

Sets the output file or the error message output file.

`version`

Returns integer information describing the version of the library, license number, operating system, and compiler.

### TIME AND DATE:

`ctime`

Returns the number of CPU seconds used.

`date_to_days`

Computes the number of days from January 1, 1900, to the given date.

`days_to_date`

Gives the date corresponding to the number of days since January 1, 1900.

### ERROR HANDLING:

`error_options`

Sets various error handling options.

`error_code`

Gets the code corresponding to the error message from the last function called.

### CONSTANTS:

`constant`

Returns the value of various mathematical and physical constants.

`machine (integer)`

Returns integer information describing the computer's arithmetic.

`machine (float)`

Returns information describing the computer's floating-point arithmetic.

**SORTING:**

<code>sort</code>	Sorts a vector by algebraic value. Optionally, a vector can be sorted by absolute value, and a sort permutation can be returned.
<code>sort (integer)</code>	Sorts an integer vector by algebraic value. Optionally, a vector can be sorted by absolute value, and a sort permutation can be returned.

**COMPUTING VECTOR NORMS:**

<code>vector_norm</code>	Computes various norms of a vector or the difference of two vectors.
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**LINEAR ALGEBRA SUPPORT:**

<code>mat_mul_rect</code>	Computes the transpose of a matrix, a matrix-vector product, a matrix-matrix product, the bilinear form, or any triple product.
<code>mat_mul_rect (complex)</code>	Computes the transpose of a matrix, the conjugate-transpose of a matrix, a matrix-vector product, a matrix-matrix product, the bilinear form, or any triple product.
<code>mat_mul_rect_band</code>	Computes the transpose of a matrix, a matrix-vector product, or a matrix-matrix product, all matrices stored in band form.
<code>mat_mul_rect_band (complex)</code>	Computes the transpose of a matrix, a matrix-vector product, or a matrix-matrix product, all matrices of complex type and stored in band form.
<code>mat_mul_rect_coordinate</code>	Computes the transpose of a matrix, a matrix-vector product, or a matrix-matrix product, all matrices stored in sparse coordinate form.
<code>mat_mul_rect_coordinate (complex)</code>	Computes the transpose of a matrix, a matrix-vector product or a matrix-matrix product, all matrices stored in sparse coordinate form.
<code>mat_add_band</code>	Adds two band matrices, both in band storage mode, $C \leftarrow \alpha A + \beta B$ .
<code>mat_add_band (complex)</code>	Adds two band complex matrices, both in band storage mode, $C \leftarrow \alpha A + \beta B$ .
<code>mat_add_coordinate</code>	Performs element-wise addition of two real matrices stored in coordinate format, $C \leftarrow \alpha A + \beta B$ .
<code>mat_add_coordinate (complex)</code>	Performs element-wise addition on two complex matrices stored in coordinate format, $C \leftarrow \alpha A + \beta B$ .
<code>matrix_norm</code>	Computes various norms of a rectangular matrix.
<code>matrix_norm_band</code>	Computes various norms of a matrix stored in band storage mode.
<code>matrix_norm_coordinate</code>	Computes various norms of a matrix stored in coordinate format.
<code>generate_test_band</code>	Generates test matrices of class $E(n, c)$ .
<code>generate_test_band (complex)</code>	Generates test matrices of class $E_c(n, c)$ .

LINEAR ALGEBRA SUPPORT: (con't)

`generate_test_coordinate` Generates test matrices of class  $D(n, c)$  and  $E(n, c)$ .

`generate_test_coordinate (complex)` Generates test matrices of class  $D(n, c)$  and  $E(n, c)$ .

**NUMERIC UTILITIES**

`c_neg` Changes the sign of a complex number.

`c_add` Adds two complex numbers.

`c_sub` Subtracts a complex number from a complex number.

`c_mul` Multiplies two complex numbers.

`c_div` Divides a complex number by a complex number.

`c_eq` Tests for equality of two complex numbers.

`cz_convert` Truncates a double precision complex number to a single precision complex number.

`zc_convert` Increases precision of a single precision complex number to a double precision complex number.

`cf_convert` Makes a complex number from an ordered pair.

`c_conjg` Conjugates a complex number.

`c_abs` Computes a magnitude of a complex number.

`c_arg` Computes an angle of a complex number.

`c_sqrt` Computes a square root of a complex number.

`c_cos` Computes a trigonometric cosine of a complex number.

`c_sin` Computes a trigonometric sine of a complex number.

`c_exp` Computes an exponential function of a complex number.

`c_log` Computes a natural logarithm of a complex number.

`cf_power` Computes a complex number raised to a real power.

`cc_power` Computes a complex number raised to a complex power.

`fi_power` Computes a real number raised to an integral power.

`ii_power` Computes an integer raised to an integral power.

## CHAPTER 1: BASIC STATISTICS

## SIMPLE SUMMARY STATISTICS:

<code>simple_statistics</code>	Computes basic univariate statistics.
<code>normal_one_sample</code>	Computes statistics for mean and variance inferences using a sample from a normal population.
<code>normal_two_sample</code>	Computes statistics for mean and variance inferences using samples from two normal populations.

## TABULATE, SORT, RANK:

<code>table_oneway</code>	Tallies observations into a one-way frequency table.
<code>table_twoway</code>	Tallies observations into a two-way frequency table.
<code>sort-data</code>	Sorts observations by specified keys, with option to tally cases into a multi-way frequency table.
<code>ranks</code>	Computes the ranks, normal scores, or exponential scores for a vector of observations.

## CHAPTER 2: REGRESSION

## MULTIVARIATE LINEAR REGRESSION—MODEL FITTING:

<code>regressors_for_glm</code>	Generates regressors for a general linear model.
<code>regression</code>	Fits a multiple linear regression model using least squares.

## MULTIVARIATE LINEAR REGRESSION—STATISTICAL INFERENCE AND DIAGNOSTICS:

<code>regression_summary</code>	Produces summary statistics for a regression model given the information from the fit.
<code>regression_prediction</code>	Computes predicted values, confidence intervals, and diagnostics after fitting a regression model.

MULTIVARIATE LINEAR REGRESSION—STATISTICAL INFERENCE  
AND DIAGNOSTICS: (cont)

`hypothesis_partial` Constructs a completely testable hypothesis.

`hypothesis_scph` Sums of cross products for a multivariate hypothesis.

`hypothesis_test` Tests for the multivariate linear hypothesis.

#### VARIABLE SELECTION:

`regression_selection` Selects the best multiple linear regression models.

`regression_stepwise` Builds multiple linear regression models using forward selection, backward selection or stepwise selection.

#### POLYNOMIAL AND NONLINEAR REGRESSION:

`poly_regression` Performs a polynomial least-squares regression.

`poly_prediction` Computes predicted values, confidence intervals, and diagnostics after fitting a polynomial regression model.

`nonlinear_regression` Fits a nonlinear regression model.

`nonlinear_optimization` Fits a nonlinear regression model using Powell's algorithm.

#### ALTERNATIVES TO LEAST SQUARES:

`Lnorm_regression` Fits a multiple linear regression model using  $L_p$  criteria other than least squares.

## CHAPTER 3: CORRELATION AND COVARIANCE

#### VARIANCES, COVARIANCES, AND CORRELATIONS:

`covariances` Computes the sample variance-covariance or correlation matrix.

`partial_covariances` Computes partial covariances or partial correlations from the covariance or correlation matrix.

`pooled_covariances` Computes a pooled variance-covariance from the observations.

`robust_covariances` Computes a robust estimate of a covariance matrix and mean vector.

## CHAPTER 4: ANALYSIS OF VARIANCE AND DESIGNED EXPERIMENTS

### GENERAL ANALYSIS OF VARIANCE:

<code>anova_oweway</code>	Analyzes a one-way classification model.
<code>anova_factorial</code>	Analyzes a balanced factorial design with fixed effects.
<code>anova_nested</code>	Analyzes a completely nested random effects model with possibly unequal numbers in the subgroups.
<code>anova_balanced</code>	Analyzes a balanced complete experimental design for a fixed, random, or mixed model.

### DESIGNED EXPERIMENTS:

<code>crd_factorial</code>	Analyzes data from balanced and unbalanced completely randomized experiments.
<code>rcbd_factorial</code>	Analyzes data from balanced and unbalanced randomized complete-block experiments.
<code>latin_square</code>	Analyzes data from latin-square experiments.
<code>lattice</code>	Analyzes balanced and partially-balanced lattice experiments.
<code>split_plot</code>	Analyzes a wide variety of split-plot experiments with fixed, mixed or random factors.
<code>split_split_plot</code>	Analyzes data from split-split-plot experiments.
<code>strip_plot</code>	Analyzes data from strip-plot experiments.
<code>strip_split_plot</code>	Analyzes data from strip-split-plot experiments.

### UTILITIES:

<code>homogeneity</code>	Conducts Bartlett's and Levene's tests of the homogeneity of variance assumption in analysis of variance.
<code>multiple_comparisons</code>	Compares differences among averages using the SNK, LSD, Tukey's, Duncan's and Bonferroni's multiple comparisons tests.
<code>yates</code>	Estimates missing observations in designed experiments using Yate's method.

## CHAPTER 5: CATEGORICAL AND DISCRETE DATA ANALYSIS

### STATISTICS IN THE TWO-WAY CONTINGENCY TABLE:

<code>contingency_table</code>	Performs a chi-squared analysis of a two-way contingency table.
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STATISTICS IN THE TWO-WAY CONTINGENCY TABLE: (con't)

`exact_enumeration` Computes exact probabilities in a two-way contingency table, using the total enumeration method.

`exact_network` Computes exact probabilities in a two-way contingency table using the network algorithm.

**GENERALIZED CATEGORICAL MODELS:**

`categorical_glm` Analyzes categorical data using logistic, Probit, Poisson, and other generalized linear models.

**CHAPTER 6: NONPARAMETRIC STATISTICS****ONE SAMPLE TESTS—NONPARAMETRIC STATISTICS:**

`sign_test` Performs a sign test.

`wilcoxon_sign_rank` Performs a Wilcoxon signed rank test.

`noether_cyclical_trend` Performs the Noether's test for cyclical trend.

`cox_stuart_trends_test` Performs the Cox and Stuart' sign test for trends in location and dispersion.

`tie_statistics` Computes tie statistics for a sample of observations.

**TWO OR MORE SAMPLES:**

`wilcoxon_rank_sum` Performs a Wilcoxon rank sign test.

`kruskal_wallis_test` Performs a Kruskal-Wallis's test for identical population medians.

`friedmans_test` Performs Friedman's test for a randomized complete block design.

`cochran_q_test` Performs Cochran's  $Q$  test for related observations.

`k_trends_test` Performs k-sample trends test against ordered alternatives.

**CHAPTER 7: TESTS OF GOODNESS OF FIT****GENERAL GOODNESS-OF-FIT-TESTS:**

`chi_squared_test` Performs a chi-squared goodness-of-fit test.

`normality_test` Performs a test for normality.

## GENERAL GOODNESS-OF-FIT-TESTS: (con't)

<code>kolmogorov_one</code>	Performs a Kolmogorov-Smirnov's one-sample test for continuous distributions.
<code>kolmogorov_two</code>	Performs a Kolmogorov-Smirnov's two-sample test.
<code>multivar_normality_test</code>	Computes Mardia's multivariate measures of skewness and kurtosis and tests for multivariate normality.

## TESTS FOR RANDOMNESS:

<code>randomness_test</code>	Performs a test for randomness.
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## CHAPTER 8: TIME SERIES AND FORECASTING

## ARIMA MODELS:

<code>arma</code>	Computes least-square estimates of parameters for an ARMA model.
<code>max_arma</code>	Exact maximum likelihood estimation of the parameters in a univariate ARMA (autoregressive, moving average) time series model.
<code>auto_uni_ar</code>	Automatic selection and fitting of a univariate autoregressive time series model. The lag for the model is automatically selected using Akaike's information criterion (AIC). Estimates of the autoregressive parameters for the model with minimum AIC are calculated using method of moments, method of least squares or maximum likelihood.
<code>ts_outlier_identification</code>	Detects and determines outliers and simultaneously estimates the model parameters in a time series whose underlying outlier-free series follows a general seasonal or nonseasonal ARMA model.
<code>ts_outlier_forecast</code>	Computes forecasts, their associated probability limits and weights for an outlier contaminated time series whose underlying outlier free series follows a general seasonal or nonseasonal ARMA model.
<code>auto_arima</code>	Automatically identifies time series outliers, determines parameters of a multiplicative seasonal ARIMA $(p,0,q)X(0,d,0)_s$ model and produces forecasts that incorporate the effects of outliers whose effects persist beyond the end of the series.
<code>arma_forecast</code>	Computes forecasts and their associated probability limits for an ARMA model.
<code>difference</code>	Differences a seasonal or nonseasonal time series.
<code>seasonal_fit</code>	Estimates the optimum seasonality parameters for a time series using an autoregressive model, $AR(p)$ , to represent the time series.

## MODEL CONSTRUCTION AND EVALUATION UTILITIES:

<code>box_cox_transform</code>	Performs a Box-Cox transformation.
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MODEL CONSTRUCTION AND EVALUATION UTILITIES: (cont)

<code>autocorrelation</code>	Computes the sample autocorrelation function of a stationary time series.
<code>crosscorrelation</code>	Computes the sample cross-correlation function of two stationary time series.
<code>multi_crosscorrelation</code>	Computes the multichannel cross-correlation function of two mutually stationary multichannel time series.
<code>partial_autocorrelation</code>	Computes the sample partial autocorrelation function of a stationary time series.
<code>lack_of_fit</code>	Performs lack-of-fit test for an univariate time series or transfer function given the appropriate correlation function.
<code>estimate_missing</code>	Estimates missing values in a time series.

**GARCH MODELING:**

<code>garch</code>	Computes estimates of the parameters of a Generalized Autoregressive Conditional Heteroskedastic (GARCH)( $p, q$ ) model.
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**FREQUENCY DOMAIN MODELING:**

<code>kalman</code>	Performs Kalman filtering and evaluates the likelihood function for the state-space model.
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**CHAPTER 9: MULTIVARIATE ANALYSIS****HIERARCHICAL CLUSTER ANALYSIS:**

<code>dissimilarities</code>	Computes a matrix of dissimilarities (or similarities) between the columns (or rows) of a matrix.
<code>cluster_hierarchical</code>	Performs a hierarchical cluster analysis given a distance matrix.
<code>cluster_number</code>	Computes cluster membership for a hierarchical cluster tree.

**K-MEANS CLUSTER ANALYSIS:**

<code>cluster_k_means</code>	Performs a $K$ -means (centroid) cluster analysis.
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**PRINCIPAL COMPONENTS:**

<code>principal_components</code>	Computes principal components.
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**FACTOR ANALYSIS:**

<code>factor_analysis</code>	Extracts initial factor-loading estimates in factor analysis with rotation options.
<code>discriminant_analysis</code>	Performs discriminant function analysis.

## CHAPTER 10: SURVIVAL AND RELIABILITY ANALYSIS

### SURVIVAL ANALYSIS:

<code>kaplan_meier_estimates</code>	Computes Kaplan-Meier estimates of survival probabilities in stratified samples.
<code>prop_hazards_gen_lin</code>	Analyzes survival and reliability data using Cox's proportional hazards model.
<code>survival_glm</code>	Analyzes survival data using a generalized linear model.
<code>survival_estimates</code>	Estimates using various parametric models.

### RELIABILITY ANALYSIS:

<code>nonparam_hazard_rate</code>	Estimates a reliability hazard function using a nonparametric approach.
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### ACTUARIAL TABLES:

<code>life_tables</code>	Produces population and cohort life tables.
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## CHAPTER 11: PROBABILITY DISTRIBUTION FUNCTIONS AND INVERSES

### DISCRETE RANDOM VARIABLES:

<code>binomial_cdf</code>	Evaluates the binomial distribution function.
<code>binomial_pdf</code>	Evaluates the binomial probability function.
<code>hypergeometric_cdf</code>	Evaluates the hypergeometric distribution function.
<code>hypergeometric_pdf</code>	Evaluates the hypergeometric probability function.
<code>poisson_cdf</code>	Evaluates the Poisson distribution function.
<code>poisson_pdf</code>	Evaluates the Poisson probability function.

### CONTINUOUS RANDOM VARIABLES:

<code>beta_cdf</code>	Evaluates the beta probability distribution function.
<code>beta_inverse_cdf</code>	Evaluates the inverse of the beta distribution function.
<code>bivariate_normal_cdf</code>	Evaluates the bivariate normal distribution function.
<code>chi_squared_cdf</code>	Evaluates the chi-squared distribution function.

CONTINUOUS RANDOM VARIABLES: (cont)

<code>chi_squared_inverse_cdf</code>	Evaluates the inverse of the chi-squared distribution function.
<code>non_central_chi_sq</code>	Evaluates the noncentral chi-squared distribution function.
<code>non_central_chi_sq_inv</code>	Evaluates the inverse of the noncentral chi-squared function.
<code>F_cdf</code>	Evaluates the $F$ distribution function.
<code>F_inverse_cdf</code>	Evaluates the inverse of the $F$ distribution function.
<code>gamma_cdf</code>	Evaluates the gamma distribution function.
<code>gamma_inverse_cdf</code>	Evaluates the inverse of the gamma distribution function.
<code>normal_cdf</code>	Evaluates the standard normal (Gaussian) distribution function.
<code>normal_inverse_cdf</code>	Evaluates the inverse of the standard normal (Gaussian) distribution function.
<code>t_cdf</code>	Evaluates the Student's $t$ distribution function.
<code>t_inverse_cdf</code>	Evaluates the inverse of the Student's $t$ distribution function.
<code>non_central_t_cdf</code>	Evaluates the noncentral Student's $t$ distribution function.
<code>non_central_t_inv_cdf</code>	Evaluates the inverse of the noncentral Student's $t$ distribution function.

## CHAPTER 12: RANDOM NUMBER GENERATION

### UNIVARIATE DISCRETE DISTRIBUTIONS:

<code>random_binomial</code>	Generates pseudorandom binomial numbers from a binomial distribution.
<code>random_geometric</code>	Generates pseudorandom numbers from a geometric distribution.
<code>random_hypergeometric</code>	Generates pseudorandom numbers from a hypergeometric distribution.
<code>random_logarithmic</code>	Generates pseudorandom numbers from a logarithmic distribution.
<code>random_neg_binomial</code>	Generates pseudorandom numbers from a negative binomial distribution.
<code>random_poisson</code>	Generates pseudorandom numbers from a Poisson distribution.
<code>random_uniform_discrete</code>	Generates pseudorandom numbers from a discrete uniform distribution.
<code>random_general_discrete</code>	Generates pseudorandom numbers from a general discrete distribution using an alias method or optionally a table lookup method.

**UNIVARIATE CONTINUOUS DISTRIBUTIONS:**

<code>random_beta</code>	Generates pseudorandom numbers from a beta distribution.
<code>random_cauchy</code>	Generates pseudorandom numbers from a Cauchy distribution.
<code>random_chi_squared</code>	Generates pseudorandom numbers from a chi-squared distribution.
<code>random_exponential</code>	Generates pseudorandom numbers from a standard exponential distribution.
<code>random_exponential_mix</code>	Generates pseudorandom mixed numbers from a standard exponential distribution.
<code>random_gamma</code>	Generates pseudorandom numbers from a standard gamma distribution.
<code>random_lognormal</code>	Generates pseudorandom numbers from a lognormal distribution.
<code>random_normal</code>	Generates pseudorandom numbers from a standard normal distribution using an inverse CDF method.
<code>random_stable</code>	Sets up a table to generate pseudorandom numbers from a general discrete distribution.
<code>random_student_t</code>	Generates pseudorandom Student's $t$ from a random distribution.
<code>random_triangular</code>	Generates pseudorandom numbers from a triangular distribution.
<code>random_uniform</code>	Generates pseudorandom numbers from a uniform (0, 1) distribution.
<code>random_von_mises</code>	Generates pseudorandom numbers from a von Mises distribution.
<code>random_weibull</code>	Generates pseudorandom numbers from a Weibull distribution.
<code>random_general_continuous</code>	Generates pseudorandom numbers from a general continuous distribution.
<code>continuous_table_setup</code>	Sets up a table to generate pseudorandom numbers from a general continuous distribution.

**MULTIVARIATE CONTINUOUS DISTRIBUTIONS:**

<code>random_normal_multivariate</code>	Generates pseudorandom numbers from a multivariate normal distribution.
<code>random_orthogonal_matrix</code>	Generates a pseudorandom orthogonal matrix or a correlation matrix.
<code>random_mvar_from_data</code>	Generates pseudorandom numbers from a multivariate distribution determined from a given sample.
<code>random_multinomial</code>	Generates pseudorandom numbers from a multinomial distribution.
<code>random_sphere</code>	Generates pseudorandom points on a unit circle or K-dimensional sphere.
<code>random_table_twoway</code>	Generates a pseudorandom two-way table.

**ORDER STATISTICS:**

`random_order_normal` Generates pseudorandom order statistics from a standard normal distribution.

`random_order_uniform` Generates pseudorandom order statistics from a uniform (0, 1) distribution.

**STOCHASTIC PROCESSES:**

`random_arma` Generates pseudorandom ARMA process numbers.

`random_npp` Generates pseudorandom numbers from a nonhomogeneous Poisson process.

**SAMPLES AND PERMUTATIONS:**

`random_permutation` Generates a pseudorandom permutation.

`random_sample_indices` Generates a simple pseudorandom sample of indices.

`random_sample` Generates a simple pseudorandom sample from a finite population.

**UTILITY FUNCTIONS:**

`random_option` Selects the uniform (0, 1) multiplicative congruential pseudorandom number generator.

`random_option_get` Retrieves the uniform (0, 1) multiplicative congruential pseudorandom number generator.

`random_seed_get` Retrieves the current value of the seed used in the IMSL random number generators.

`random_substream_seed_get` Retrieves a seed for the congruential generators that do not do shuffling that will generate random numbers beginning 100,000 numbers farther along.

`random_seed_set` Initializes a random seed for use in the IMSL random number generators.

`random_table_set` Sets the current table used in the shuffled generator.

`random_table_get` Retrieves the current table used in the shuffled generator.

`random_GFSR_table_set` Sets the current table used in the GFSR generator.

`random_GFSR_table_get` Retrieves the current table used in the GFSR generator.

`random_MT32_init` Initializes the 32-bit Mersenne Twister generator using an array.

`random_MT32_table_get` Retrieves the current table used in the 32-bit Mersenne Twister generator.

`random_MT32_table_set` Sets the current table used in the 32-bit Mersenne Twister generator.

`random_MT64_init` Initializes the 64-bit Mersenne Twister generator using an array.

CONTINUOUS RANDOM VARIABLES: (cont)

`random_MT64_table_get` Retrieves the current table used in the 64-bit Mersenne Twister generator.

`random_MT64_table_set` Sets the current table used in the 64-bit Mersenne Twister generator.

**LOW-DISCREPANCY SEQUENCE:**

`faure_next_point` Computes a shuffled Faure sequence.

**CHAPTER 13: NEURAL NETWORKS****NETWORK:**

`mlff_network` Creates a multilayered feedforward neural network.

`mlff_network_trainer` Trains a multilayered feedforward neural network.

`mlff_network_forecast` Calculates forecasts for trained multilayered feedforward neural networks.

**PREPROCESSING FILTERS:**

`scale_filter` Scales or unscales continuous data prior to its use in neural network training, testing, or forecasting.

`time_series_filter` Converts time series data to the format required for processing by a neural network.

`time_series_class_filter` Converts time series data sorted within nominal classes in decreasing chronological order to a useful format for processing by a neural network.

`unsupervised_nominal_filter` Converts nominal data into a series of binary encoded columns for input to a neural network. Optionally, it can also reverse the binary encoding, accepting a series of binary encoded columns and returning a single column of nominal classes.

`unsupervised_ordinal_filter` Converts ordinal data into proportions. Optionally, it can also reverse encoding, accepting proportions and converting them into ordinal values.

**CHAPTER 14: PRINTING FUNCTIONS****PRINT:**

`write_matrix` Prints a rectangular matrix (or vector) stored in contiguous memory locations.

**SET:**

`page` Sets or retrieves the page width or length.

`write_options` Sets or retrieves an option for printing a matrix.

## CHAPTER 15: UTILITIES

### SET OUPUT FILES:

<code>output_file</code>	Sets the output file or the error message output file.
<code>version</code>	Returns integer information describing the version of the library, license number, operating system, and compiler.

### ERROR HANDLING:

<code>error_options</code>	Sets various error handling options.
<code>error_code</code>	Returns the code corresponding to the error message from the last function called.

### CONSTANTS:

<code>machine (integer)</code>	Returns integer information describing the computer's arithmetic.
<code>machine (float)</code>	Returns information describing the computer's floating-point arithmetic.
<code>data_sets</code>	Retrieves a commonly analyzed data set.

### MATHEMATICAL SUPPORT:

<code>mat_mul_rect</code>	Computes the transpose of a matrix, a matrix-vector product, a matrix-matrix product, a bilinear form, or any triple product.
<code>permute_vector</code>	Rearranges the elements of a vector as specified by a permutation.
<code>permute_matrix</code>	Permutates the rows or columns of a matrix.
<code>binomial_coefficient</code>	Evaluates the binomial coefficient.
<code>beta</code>	Evaluates the complete beta function.
<code>beta_incomplete</code>	Evaluates the real incomplete beta function.
<code>log_beta</code>	Evaluates the log of the real beta function.
<code>gamma</code>	Evaluates the real gamma function.
<code>gamma_incomplete</code>	Evaluates the incomplete gamma function.
<code>log_gamma</code>	Evaluates the logarithm of the absolute value of the gamma function.
<code>ctime</code>	Returns the number of CPU seconds used.